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ANNEXES 1 to 2

ANNEXES

to the

Commission Regulation

amending Regulation (EC) No 692/2008 as regards emissions from light passenger and commercial vehicles (Euro 6)

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ANNEX I

In Appendix 6 to Annex I to Regulation (EC) No 692/2008, table 1 is amended as follows:

(1) rows ZD, ZE, ZF are replaced by the following:

"

ZD	Euro 6c	Euro 6-2	M, N1 class I	PI, CI		1.9.2018	31.8.2019
ZE	Euro 6c	Euro 6-2	N1 class II	PI, CI		1.9.2019	31.8.2020
ZF	Euro 6c	Euro 6-2	N1 class III, N2	PI, CI		1.9.2019	31.8.2020

";

(2) the following rows are inserted after row ZF:

"

ZG	Euro 6d-TEMP	Euro 6-2	M, N1 class I	PI, CI	1.9.2017	1.9.2019	31.12.2019
ZH	Euro 6d-TEMP	Euro 6-2	N1 class II	PI, CI	1.9.2018	1.9.2020	31.12.2020
ZI	Euro 6d-TEMP	Euro 6-2	N1 class III, N2	PI, CI	1.9.2018	1.9.2020	31.12.2020
ZJ	Euro 6d	Euro 6-2	M, N1 class I	PI, CI	1.1.2020	1.1.2021	
ZK	Euro 6d	Euro 6-2	N1 class II	PI, CI	1.1.2021	1.1.2022	
ZL	Euro 6d	Euro 6-2	N1 class III, N2	PI, CI	1.1.2021	1.1.2022	

";

(3) in the key to the table, the following paragraphs are inserted after the paragraph concerning the 'Euro 6b' emissions standard:

'Euro 6c' emissions standard = Full Euro 6 emission requirements without RDE testing, i.e. Euro 6b emission standard and final particle number standards for PI vehicles and use of E10 and B7 reference fuel (where applicable) assessed on regulatory lab test cycle,

‘Euro 6d-TEMP’ emissions standard = Full Euro 6 emission requirements, i.e. Euro 6b emission standard and final particle number standards for PI vehicles and use of E10 and B7 reference fuel (where applicable) assessed on regulatory lab test cycle, RDE testing against temporary conformity factors;”;

(4) in the key to the table, the paragraph concerning the ‘Euro 6c’ emissions standard is replaced by the following:

“Euro 6d’ emissions standard = Full Euro 6 emission requirements, i.e. Euro 6b emission standard and final particle number standards for PI vehicles and use of E10 and B7 reference fuel (where applicable) assessed on regulatory lab test cycle, RDE testing against final conformity factors;”.

ANNEX II

Annex IIIa to Regulation (EC) No 692/2008 is amended as follows:

(1) point 2.1 is replaced by the following:

"2.1 Not-to-exceed emission limits

Throughout the normal life of a vehicle type approved according to Regulation (EC) No 715/2007, its emissions determined in accordance with the requirements of this Annex and emitted at any possible RDE test performed in accordance with the requirements of this Annex, shall not be higher than the following not-to-exceed (NTE) values:

$$NTE_{pollutant} = CF_{pollutant} \times TF(p_1, \dots, p_n) \times \text{EURO-6},$$

where EURO-6 is the applicable Euro 6 emission limit laid down in Table 2 of Annex I to Regulation (EC) No 715/2007. ”;

(2) the following points 2.1.1, 2.1.2 and 2.1.3 are inserted:

"2.1.1 Final Conformity Factors

The conformity factor $CF_{pollutant}$ for the respective pollutant is specified as follows:

Pollutant	Mass of oxides of nitrogen (NOx)	Number of particles (PN)	Mass of carbon monoxide (CO) ⁽¹⁾	Mass of total hydrocarbons (THC)	Combined mass of total hydrocarbons and oxides of nitrogen (THC + NOx)
$CF_{pollutant}$	1 + <i>margin</i> with <i>margin</i> = 0,5	to be determined	-	-	-

⁽¹⁾ CO emissions shall be measured and recorded at RDE tests.

margin is a parameter taking into account the additional measurement uncertainties introduced by the PEMS equipment, which are subject to an annual review and shall be revised as a result of the improved quality of the PEMS procedure or technical progress.

2.1.2 Temporary Conformity Factors

By way of exception to the provisions of point 2.1.1, during a period of 5 years and 4 months following the dates specified in Article 10(4) and (5) of Regulation (EC) 715/2007 and upon request of the manufacturer, the following temporary conformity factors may apply:

Pollutant	Mass of oxides of nitrogen (NOx)	Number of particles (PN)	Mass of carbon monoxide (CO) ⁽¹⁾	Mass of total hydrocarbons (THC)	Combined mass of total hydrocarbons and oxides of nitrogen (THC + NOx)
$CF_{pollutant}$	2,1	to be determined	-	-	-

(1) CO emissions shall be measured and recorded at RDE tests.

The application of temporary conformity factors shall be recorded in the certificate of conformity of the vehicle.

2.1.3 Transfer functions

The transfer function $TF(p_1, \dots, p_n)$ referred to in point 2.1 is set to 1 for the entire range of parameters p_i ($i = 1, \dots, n$).

If the transfer function $TF(p_1, \dots, p_n)$ is amended, this shall be done in a manner which is not detrimental to the environmental impact and the effectiveness of the RDE test procedures. In particular the following condition shall hold:

$$\int TF(p_1, \dots, p_n) * Q(p_1, \dots, p_n) dp = \int Q(p_1, \dots, p_n) dp$$

Where:

- dp represents the integral over the entire space of the parameters p_i ($i = 1, \dots, n$)
- $Q(p_1, \dots, p_n)$, is the probability density of an event corresponding to the parameters p_i ($i = 1, \dots, n$) in real driving.";

“

(3) the following point 3.1.0 is inserted:

"3.1.0 The requirements of point 2.1 shall be fulfilled for the urban part and the complete PEMS trip. Upon the choice of the manufacturer the conditions of at least one of the two points below shall be fulfilled:

3.1.0.1 $M_{gas,d,t} \leq NTE_{pollutant}$ and $M_{gas,d,u} \leq NTE_{pollutant}$ with the definitions of point 2.1 of this Annex and points 6.1 and 6.3 of Appendix 5 and the setting $gas = pollutant$.

3.1.0.2 $M_{w, gas, d} \leq NTE_{pollutant}$ and $M_{w, gas, d, U} \leq NTE_{pollutant}$ with the definitions of point 2.1 of this Annex and point 3.9 of Appendix 6 and the setting $gas = pollutant$.

"

(4) point 5.3 is deleted;

(5) point 5.4 is replaced by the following:

"5.4. Dynamic conditions

The dynamic conditions encompass the effect of road grade, head wind and driving dynamics (accelerations, decelerations) and auxiliary systems upon energy consumption and emissions of the test vehicle. The verification of the normality of dynamic conditions shall be done after the test is completed, using the recorded PEMS data. This verification shall be conducted in 2 steps:

5.4.1 The overall excess or insufficiency of driving dynamics during the trip shall be checked using the methods described in Appendix 7a to this Annex.

5.4.2 If the trip results as valid following the verifications according to point 5.4.1, the methods for verifying the normality of the dynamic conditions and laid down in Appendices 5 and 6 to this Annex must be applied. Each method includes a reference for dynamic conditions, ranges around the reference and the minimum coverage requirements to achieve a valid test.";

(6) point 6.8 is replaced by the following:

"6.8 The average speed (including stops) of the urban driving part of the trip should be between 15 and 40 km/h. Stop periods, defined as vehicle speed of less than 1 km/h, shall account for 6-30% of the time duration of urban operation. Urban operation shall contain several stop periods of 10s or longer. If a stop period lasts more the 180 s, the emission events during the 180 s following such excessively long stop period shall be excluded from the evaluation.";

(7) in point 6.11, the following sentence is added:

"In addition, the proportional cumulative positive altitude gain shall be less than 1200 m/100km) and be determined according to Appendix 7b.";

(8) point 9.5 is replaced by the following:

"9.5. If during a particular time interval the ambient conditions are extended in accordance with point 5.2, the emissions during this particular time interval, calculated according to Appendix 4, shall be divided by a value of 1,6 before being evaluated for compliance with the requirements of this Annex.";

(9) Appendix 1 is amended as follows:

(a) in point 3.4.6, the following sentence is added:

"It is permitted to power any safety-related illumination of fixtures and installations of PEMS components outside of the vehicle's cabin by the vehicle's battery.";

(b) in point 4.5, the following sentence is added:

"To minimize analyser drift, one should conduct the zero and span calibration of analysers at an ambient temperature that resembles, as closely as possible, the temperature experienced by the test equipment during the RDE trip.";

(10) in Appendix 2, footnote 2 to table 4 in point 8 is replaced by the following:

"This general requirement applies to the speed sensor only; if vehicle speed is used to determine parameters like acceleration, the product of speed and positive acceleration, or RPA, the speed signal shall have an accuracy of 0,1 % above 3 km/h and a sampling frequency of 1 Hz. This accuracy requirement can be met by using the signal of a wheel rotational speed sensor.";

(11) in Appendix 6 point 2 the definition

"a_iActual acceleration in time step i, if not other defined in an equation:

$$a_i = \frac{(v_{i+1} - v_i)}{3.6 \times (t_{i+1} - t_i)}, [m/s^2]$$

is deleted.

(12) in Appendix 6 point 2 the following definitions are inserted

"

$\bar{m}_{gas,U}$ Weighted emission value of an exhaust gas component “gas” for the subsample of all seconds i with v_i < 60 km/h, g/s

M_{w,gas,d,U} Weighted distance-specific emissions for the exhaust gas component “gas” for the subsample of all seconds i with v_i < 60 km/h, g/km

\bar{v}_U Weighted vehicle speed in the wheel power class j, km/h

"

(13) in Appendix 6 point 3.1 the first paragraph is replaced by the following text:

"

The actual wheel power P_{r,i} shall be the total power to overcome air resistance, rolling resistance, road gradients, longitudinal inertia of the vehicle and rotational inertia of the wheels.

"

(14) in Appendix 6 point 3.2 is replaced by the following text:

"

3.2 Classification of the moving averages to urban, rural and motorway

The standard power frequencies are defined for urban driving and for the total trip (see paragraph 3.4) and a separate evaluation of the emissions shall be made for the total trip and for the urban part. The three second moving averages calculated according to paragraph 3.3 shall therefore be allocated later to urban and extra-urban driving conditions according to the velocity signal (v_i) from the actual second i as outlined in Table 1-1.

Table 1-1

Speed ranges for the allocation of test data to urban, rural and motorway conditions in the power binning method

	Urban	Rural	Motorway
v _i [km/h]	0 to ≤ 60	>60 to ≤ 90	>90

"

(15) in Appendix 6 point 3.9 is replaced by the following text:

"

3.9 Calculation of the weighted distance-specific emission value

The time based weighted averages of the emissions in the test shall be converted into distance based emissions once for the urban data set and once for the total data set as follows:

For the total trip:
$$M_{w, gas, d} = 1000 \cdot \frac{\bar{m}_{gas} \times 3600}{V}$$

For the urban part of the trip:
$$M_{w, gas, d, U} = 1000 \cdot \frac{\bar{m}_{gas, U} \times 3600}{V_U}$$

Using these formulas, weighted averages shall be calculated for the following pollutants for the total trip and for the urban part of the trip:

$M_{w, NOx, d}$ weighted NOx test result in [mg/km]

$M_{w, NOx, d, U}$ weighted NOx test result in [mg/km]

$M_{w, CO, d}$ weighted CO test result in [mg/km]

$M_{w, CO, d, U}$ weighted CO test result in [mg/km]

"

(16) the following Appendices 7a and 7b are inserted:

"Appendix 7a

Verification of overall trip dynamics

1. INTRODUCTION

This Appendix describes the calculation procedures to verify the overall trip dynamics, to determine the overall excess or absence of dynamics during urban, rural and motorway driving.

2. SYMBOLS

RPA Relative Positive Acceleration

“acceleration resolution a_{res} ” minimum acceleration >0 measured in m/s^2

T4253H compound data smoother

“positive acceleration a_{pos} ” acceleration [m/s^2] greater than $0.1 m/s^2$

Index (i) refers to the time step

Index (j) refers to the time step of positive acceleration datasets

Index (k) refers to the category (t=total, u=urban, r=rural, m=motorway)

Δ	-	difference
$>$	-	larger
\geq	-	larger or equal
$\%$	-	per cent
$<$	-	smaller
\leq	-	smaller or equal
a	-	acceleration [m/s ²]
a_i	-	acceleration in time step i [m/s ²]
a_{pos}	-	positive acceleration greater than 0.1 m/s ² [m/s ²]
$a_{pos,l,k}$	-	positive acceleration greater than 0.1 m/s ² in time step i considering the urban, rural and motorway shares [m/s ²]
a_{res}	-	acceleration resolution [m/s ²]
d_i	-	distance covered in time step i [m]
$d_{l,k}$	-	distance covered in time step i considering the urban, rural and motorway shares [m]
M_k	-	number of samples for urban, rural and motorway shares with positive acceleration greater than 0.1 m/s ²
N_k	-	total number of samples for the urban, rural and motorway shares and the complete trip
r_{max}	-	acceleration resolution threshold for vehicle speed data quality
RPA_k	-	relative positive acceleration for urban, rural and motorway shares [m/s ² or kW/(kg*km)]
t_k	-	duration of the urban, rural and motorway shares and the complete trip [s]
v	-	vehicle speed [km/h]
v_i	-	actual vehicle speed in time step i [km/h]
$v_{l,k}$	-	actual vehicle speed in time step i considering the urban, rural and motorway shares [km/h]
$(v \cdot a)_i$	-	actual vehicle speed per acceleration in time step i [m ² /s ³ or W/kg]
$(v \cdot a_{pos})_{j,k}$	-	actual vehicle speed per positive acceleration greater than 0.1 m/s ² in time step j considering the urban, rural and motorway shares [m ² /s ³]

or

W/kg].

$(v \cdot a_{pos})_{k-[95]}$ - 95th percentile of the product of vehicle speed per positive acceleration greater than 0.1 m/s² for urban, rural and motorway shares [m²/s³ or W/kg]

\bar{v}_k - average vehicle speed for urban, rural and motorway shares [km/h]

3. TRIP INDICATORS

3.1. Calculations

3.1.1. Data pre-processing

Dynamic parameters like acceleration, $v \cdot a_{pos}$ or RPA shall be determined with a speed signal of an accuracy of 0.1% above 3 km/h and a sampling frequency of 1 Hz. This accuracy requirement is generally fulfilled by wheel (rotational) speed signals.

The speed trace shall be checked for faulty or implausible sections. The vehicle speed trace of such sections is characterised by steps, jumps, terraced speed traces or missing values. In a second step the acceleration values shall be ranked in ascending order, in order to determine the acceleration resolution a_{res} (minimum acceleration value > 0).

- If $a_{res} \leq 0.01 \text{ m/s}^2$, the vehicle speed measurement is accurate enough.
- If $0.01 < a_{res} \leq r_{max} \text{ m/s}^2$, smoothing by using a T4253H Hanning filter.
- If $a_{res} > r_{max} \text{ m/s}^2$, the trip is invalid.

The T4235 Hanning filter performs the following calculations: The smoother starts with a running median of 4, which is centered by a running median of 2. It then resmooths these values by applying a running median of 5, a running median of 3, and hanning (running weighted averages). Residuals are computed by subtracting the smoothed series from the original series. This whole process is then repeated on the computed residuals. Finally, the smoothed residuals are computed by subtracting the smoothed values obtained the first time through the process.

If smoothing was applied, the smoothed speed trace builds the basis for further calculations and binning and the acceleration values need to be recalculated on the basis of the smoothed speed trace as described in paragraph 3.1.2.

3.1.2. Calculation of distance, acceleration and $v \cdot a$

The following calculations shall be performed over the whole time based speed trace (1 Hz resolution) from second 1 to second t_T (last second).

The distance increment per data sample shall be calculated as follows:

$$d_i = v_i/3.6, \quad i = 1 \text{ to } N_t$$

Where:

d_i is the distance covered in time step i [m]

v_i is the actual vehicle speed in time step i [km/h]

N_t is the total number of samples

The acceleration shall be calculated as follows:

$$a_i = (v_{i+1} - v_{i-1})/(2 \cdot 3.6), \quad i = 1 \text{ to } N_t$$

Where:

a_i is the acceleration in time step i [m/s^2]. For $i = 1$: $v_{i-1} = 0$, for $i = N_t$: $v_{i+1} = 0$.

The product of vehicle speed per acceleration shall be calculated as follows:

$$(v \cdot a)_i = v_i \cdot a_i/3.6, \quad i = 1 \text{ to } N_t$$

Where:

$(v \cdot a)_i$ is the product of the actual vehicle speed per acceleration in time step i [m^2/s^3 or W/kg].

3.1.3. Binning of the results

After the calculation of a_i and $(v \cdot a)_i$, the values v_i , d_i , a_i and $(v \cdot a)_i$ shall be ranked in ascending order of the vehicle speed.

All datasets with $v_i \leq 60 \text{ km/h}$ belong to the “urban” speed bin, all datasets with $60 \text{ km/h} < v_i \leq 90 \text{ km/h}$ belong to the “rural” speed bin and all datasets with $v_i > 90 \text{ km/h}$ belong to the “motorway” speed bin.

The number of datasets with acceleration values $a_i > 0.1 \text{ m/s}^2$ shall be bigger or equal to 150 in each speed bin.

For each speed bin the average vehicle speed \bar{v}_k shall be calculated as follows:

$$\bar{v}_k = (\sum_i v_{i,k})/N_k, \quad i = 1 \text{ to } N_k, k = u, r, m$$

Where:

N_k is the total number of samples of the urban, rural, and motorway shares.

3.1.4. Calculation of $v \cdot a_{pos}$ -[95] per speed bin

The 95th percentile of the $v \cdot a_{pos}$ values shall be calculated as follows:

The $(v \cdot a)_{i,k}$ values in each speed bin shall be ranked in ascending order for all datasets with $a_{i,k} \geq 0.1 \text{ m/s}^2$ and the total number of these samples M_k shall be determined.

Percentile values are then assigned to the $(v \cdot a_{pos})_{j,k}$ values with $a_{i,k} \geq 0.1 \text{ m/s}^2$ as follows:

The lowest $v \cdot a_{pos}$ value gets the percentile $1/M_k$, the second lowest $2/M_k$, the third lowest $3/M_k$ and the highest value $M_k/M_k = 100\%$.

$(v \cdot a_{pos})_{k-}[95]$ is the $(v \cdot a_{pos})_{j,k}$ value, with $j/M_k = 95\%$. If $j/M_k = 95\%$ cannot be met, $(v \cdot a_{pos})_{k-}[95]$ shall be calculated by linear interpolation between consecutive samples j and $j+1$ with $j/M_k < 95\%$ and $(j+1)/M_k > 95\%$.

The relative positive acceleration per speed bin shall be calculated as follows:

$$RPA_k = \sum_j (\Delta t \cdot (v \cdot a_{pos})_{j,k}) / \sum_t d_{t,k}, \quad j = 1 \text{ to } M_k, t = 1 \text{ to } N_k, k = u, r, m$$

Where:

RPA_k is the relative positive acceleration for urban, rural and motorway shares in [m/s^2 or $\text{kWs}/(\text{kg} \cdot \text{km})$]

Δt time difference equal to 1 second

M_k the sample number for urban, rural and motorway shares with positive acceleration

N_k the total sample number for urban, rural and motorway shares

4. VERIFICATION OF TRIP VALIDITY

4.1.1. Verification of $v \cdot a_{pos}$ -[95] per speed bin (with v in $[\text{km/h}]$)

If $\bar{v}_k \leq 74.6 \text{ km/h}$ and

$$(v \cdot a_{pos})_{k-}[95] > (0.136 \cdot \bar{v}_k + 14.44)$$

is fulfilled, the trip is invalid.

If $\bar{v}_k > 74.6 \text{ km/h}$ and $(v \cdot a_{pos})_{k-}[95] > (0.0742 \cdot \bar{v}_k + 18.966)$ is fulfilled, the trip is invalid.

4.1.2. Verification of RPA per speed bin

If $\bar{v}_k \leq 94.05 \text{ km/h}$ and $RPA_k < (-0.0016 \cdot \bar{v}_k + 0.1755)$ is fulfilled, the trip is invalid.

If $\bar{v}_k > 94.05 \text{ km/h}$ and $RPA_k < 0.025$ is fulfilled, the trip is invalid.

Appendix 7b

Procedure to determine the cumulative positive elevation gain of a trip

1. INTRODUCTION

This Appendix describes the procedure to determine the cumulative elevation gain of a RDE trip.

2. SYMBOLS

$d(0)$	-	distance at the start of a trip [m]
d	-	cumulative distance travelled at the discrete way point under consideration [m]
d_0	-	cumulative distance travelled until the measurement directly before the respective way point d [m]
d_1	-	cumulative distance travelled until the measurement directly after the respective way point d [m]
d_a	-	reference way point at $d(0)$ [m]
d_e	-	cumulative distance travelled until the last discrete way point [m]
d_i	-	instantaneous distance [m]
d_{tot}	-	total test distance [m]
$h(0)$	-	vehicle altitude after the screening and principle verification of data quality at the start of a trip [m above sea level]
$h(t)$	-	vehicle altitude after the screening and principle verification of data quality at point t [m above sea level]
$h(d)$	-	vehicle altitude at the way point d [m above sea level]
$h(t-1)$	-	vehicle altitude after the screening and principle verification of data quality at point $t-1$ [m above sea level]
$h_{\text{corr}}(0)$	-	corrected altitude directly before the respective way point d [m above sea level]
$h_{\text{corr}}(1)$	-	corrected altitude directly after the respective way point d [m above sea level]
$h_{\text{corr}}(t)$	-	corrected instantaneous vehicle altitude at data point t [m above sea level]
$h_{\text{corr}}(t-1)$	-	corrected instantaneous vehicle altitude at data point $t-1$ [m above sea level]
$h_{\text{GPS},i}$	-	instantaneous vehicle altitude measured with GPS [m above sea level]
$h_{\text{GPS}}(t)$	-	vehicle altitude measured with GPS at data point t [m above sea level]
$h_{\text{int}}(d)$	-	interpolated altitude at the discrete way point under

$h_{\text{int,sm},1}(d)$	-	consideration d [m above sea level] smoothed interpolated altitude, after the first smoothing run at the discrete way point under consideration d [m above sea level]
$h_{\text{map}}(t)$	-	vehicle altitude based on topographic map at data point t [m above sea level]
Hz	-	hertz
km/h	-	kilometer per hour
m	-	meter
$\text{road}_{\text{grade},1}(d)$	-	smoothed road grade at the discrete way point under consideration d after the first smoothing run [m/m]
$\text{road}_{\text{grade},2}(d)$	-	smoothed road grade at the discrete way point under consideration d after the second smoothing run [m/m]
\sin	-	trigonometric sine function
t	-	time passed since test start [s]
t_0	-	time passed at the measurement directly located before the respective way point d [s]
v_i	-	instantaneous vehicle speed [km/h]
$v(t)$	-	vehicle speed of data point t [km/h]

3. GENERAL REQUIREMENTS

The cumulative positive elevation gain of a RDE trip shall be determined based on three parameters: the instantaneous vehicle altitude $h_{\text{GPS},i}$ [m above sea level] as measured with the GPS, the instantaneous vehicle speed v_i [km/h] recorded at a frequency of 1 Hz and the corresponding time t [s] that has passed since test start.

4. CALCULATION OF CUMULATIVE POSITIVE ELEVATION GAIN

4.1. General

The cumulative positive elevation gain of a RDE trip shall be calculated as a three-step procedure, consisting of (i) the screening and principle verification of data quality, (ii) the correction of instantaneous vehicle altitude data, and (iii) the calculation of the cumulative positive elevation gain.

4.2. Screening and principle verification of data quality

The instantaneous vehicle speed data shall be checked for completeness. Correcting for missing data is permitted if gaps remain within the requirements specified in Point 7 of Appendix 4; else, the test results shall be voided. The instantaneous altitude data shall be checked for completeness. Data gaps shall be completed by data interpolation. The correctness of interpolated data shall be verified by a topographic map. It is recommended to correct interpolated data if the following condition applies:

$$|h_{\text{GPS}}(t) - h_{\text{map}}(t)| > 40\text{m}$$

The altitude correction shall be applied so that:

$$h(t) = h_{\text{map}}(t)$$

where:

- $h(t)$ - vehicle altitude after the screening and principle verification of data quality at data point t [m above sea level]
- $h_{GPS}(t)$ - vehicle altitude measured with GPS at data point t [m above sea level]
- $h_{map}(t)$ - vehicle altitude based on topographic map at data point t [m above sea level]

4.3. Correction of instantaneous vehicle altitude data

The altitude $h(0)$ at the start of a trip at $d(0)$ shall be obtained by GPS and verified for correctness with information from a topographic map. The deviation shall not be larger than 40 m. Any instantaneous altitude data $h(t)$ shall be corrected if the following condition applies:

$$|h(t) - h(t - 1)| > (v(t)/3.6 * \sin 45^\circ)$$

The altitude correction shall be applied so that:

$$h_{corr}(t) - h_{corr}(t - 1)$$

where:

- $h(t)$ - vehicle altitude after the screening and principle verification of data quality at data point t [m above sea level]
- $h(t-1)$ - vehicle altitude after the screening and principle verification of data quality at data point t-1 [m above sea level]
- $v(t)$ - vehicle speed of data point t [km/h]
- $h_{corr}(t)$ - corrected instantaneous vehicle altitude at data point t [m above sea level]
- $h_{corr}(t-1)$ - corrected instantaneous vehicle altitude at data point t-1 [m above sea level]

Upon the completion of the correction procedure, a valid set of altitude data is established. This data set shall be used for the final calculation of the cumulative positive elevation gain as described in Point 4.4.

4.4. Final calculation of the cumulative positive elevation gain

4.4.1. Establishment of a uniform spatial resolution

The total distance d_{tot} [m] covered by a trip shall be determined as sum of the instantaneous distances d_i . The instantaneous distance d_i shall be determined as:

$$d_i = \frac{v_i}{3.6}$$

Where:

- d_i - instantaneous distance [m]
- v_i - instantaneous vehicle speed [km/h]

The cumulative elevation gain shall be calculated from data of a constant spatial resolution of 1 m starting with the first measurement at the start of a trip $d(0)$. The discrete data points at a resolution of 1 m are referred to as way points, characterized by a specific distance value d (e.g., 0, 1, 2, 3 m...) and their corresponding altitude $h(d)$ [m above sea level].

The altitude of each discrete way point d shall be calculated through interpolation of the instantaneous altitude $h_{corr}(t)$ as:

$$h_{int}(d) = h_{corr}(0) + \frac{h_{corr}(1) - h_{corr}(0)}{d_1 - d_0} * (d - d_0)$$

Where:

$h_{int}(d)$	-	interpolated altitude at the discrete way point under consideration d [m above sea level]
$h_{corr}(0)$	-	corrected altitude directly before the respective way point d [m above sea level]
$h_{corr}(1)$	-	corrected altitude directly after the respective way point d [m above sea level]
d	-	cumulative distance traveled until the discrete way point under consideration d [m]
d_0	-	cumulative distance travelled until the measurement located directly before the respective way point d [m]
d_1	-	cumulative distance travelled until the measurement located directly after the respective way point d [m]

4.4.2. Additional data smoothing

The altitude data obtained for each discrete way point shall be smoothed by applying a two-step procedure; d_a and d_e denote the first and last data point respectively (Figure 1). The first smoothing run shall be applied as follows:

$$road_{grade,1}(d) = \frac{h_{int}(d + 200m) - h_{int}(d_a)}{(d + 200m)} \quad \text{for } d \leq 200m$$

$$road_{grade,1}(d) = \frac{h_{int}(d + 200m) - h_{int}(d - 200m)}{(d + 200m) - (d - 200m)} \quad \text{for } 200m < d < (d_e - 200m)$$

$$road_{grade,1}(d) = \frac{h_{int}(d_e) - h_{int}(d - 200m)}{d_e - (d - 200m)} \quad \text{for } d \geq (d_e - 200m)$$

$$h_{int,sm,1}(d) = h_{int,sm,1}(d - 1m) + road_{grade,1}(d), d = d_a + 1 \text{ to } d_e$$

$$h_{int,sm,1}(d_a) = h_{int}(d_a) + road_{grade,1}(d_a)$$

Where:

$road_{grade,1}(d)$	-	smoothed road grade at the discrete way point under consideration after the first smoothing run [m/m]
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$h_{\text{int}}(d)$	-	interpolated altitude at the discrete way point under consideration d [m above sea level]
$h_{\text{int,sm},1}(d)$	-	smoothed interpolated altitude, after the first smoothing run at the discrete way point under consideration d [m above sea level]
d	-	cumulative distance travelled at the discrete way point under consideration [m]
d_a	-	reference way point at a distance of zero meters [m]
d_e	-	cumulative distance travelled until the last discrete way point [m]

The second smoothing run shall be applied as follows:

$$road_{\text{grade},2}(d) = \frac{h_{\text{int,sm},1}(d + 200\text{m}) - h_{\text{int,sm},1}(d_a)}{(d + 200\text{m})} \quad \text{for } d \leq 200\text{m}$$

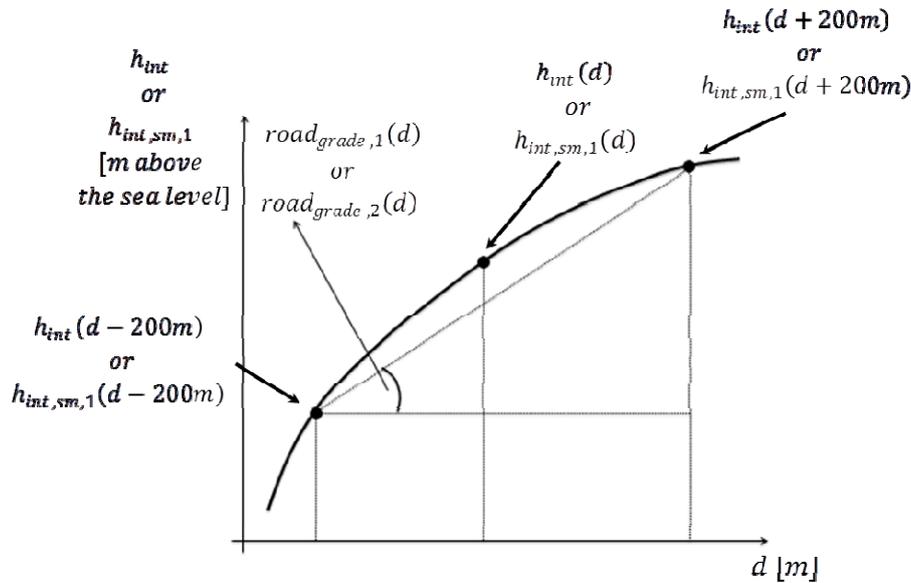
$$road_{\text{grade},2}(d) = \frac{h_{\text{int,sm},1}(d + 200\text{m}) - h_{\text{int,sm},1}(d - 200\text{m})}{(d + 200\text{m}) - (d - 200\text{m})} \quad \text{for } 200\text{m} < d < (d_e - 200\text{m})$$

$$road_{\text{grade},2}(d) = \frac{h_{\text{int,sm},1}(d_e) - h_{\text{int,sm},1}(d - 200\text{m})}{d_e - (d - 200\text{m})} \quad \text{for } d \geq (d_e - 200\text{m})$$

Where:

$road_{\text{grade},2}(d)$	-	smoothed road grade at the discrete way point under consideration after the second smoothing run [m/m]
$h_{\text{int,sm},1}(d)$	-	smoothed interpolated altitude, after the first smoothing run at the discrete way point under consideration d [m above sea level]
d	-	cumulative distance travelled at the discrete way point under consideration [m]
d_a	-	reference way point at a distance of zero meters [m]
d_e	-	cumulative distance travelled until the last discrete way point [m]

Figure 1
Illustration of the procedure to smooth the interpolated altitude signals



4.4.3. Calculation of the final result

The positive cumulative elevation gain of a trip shall be calculated by integrating all positive interpolated and smoothed road grades, i.e. $road_{grade,2}(d)$. The result should be normalized by the total test distance d_{tot} and expressed in meters of cumulative elevation gain per one hundred kilometers of distance.

1. NUMERICAL EXAMPLE

Tables 1 and 2 show the steps performed in order to calculate the positive elevation gain on the basis of data recorded during an on-road test performed with PEMS. For the sake of brevity an extract of 800m and 160s is presented here.

1.1. Screening and principle verification of data quality

The screening and principle verification of data quality consists of two steps. First, the completeness of vehicle speed data is checked. No data gaps related to vehicle speed are detected in the present data sample (see Table 1). Second, the altitude data are checked for completeness; in the data sample, altitude data related to seconds 2 and 3 are missing. The gaps are filled by interpolating the GPS signal. In addition, the GPS altitude is verified by a topographic map; this verification includes the altitude $h(0)$ at the start of the trip. Altitude data related to seconds 112 -114 are corrected on the basis of the topographic map to satisfy the following condition:

$$h_{GPS}(t) - h_{map}(t) < -40m$$

As result of the applied data verification, the data in the fifth column $h(t)$ are obtained.

1.2. Correction of instantaneous vehicle altitude data

As a next step, the altitude data $h(t)$ of seconds 1 to 4, 111 to 112 and 159 to 160 are corrected assuming the altitude values of seconds 0, 110 and 158 respectively since the following condition applies:

$$|h(t) - h(t - 1)| > (v(t)/3.6 * \sin 45^\circ)$$

As result of the applied data correction, the data in the sixth column $h_{corr}(t)$ are obtained. The effect of the applied verification and correction steps on the altitude data is depicted in Figure 2.

1.3. Calculation of the cumulative positive elevation gain

1.3.1. Establishment of a uniform spatial resolution

The instantaneous distance d_i is calculated by dividing the instantaneous vehicle speed measured in km/h by 3.6 (Column 7 in Table 1). Recalculating the altitude data to obtain a uniform spatial resolution of 1 m yields the discrete way points d (Column 1 in Table 2) and their corresponding altitude values $h_{int}(d)$ (Column 7 in Table 2). The altitude of each discrete way point d is calculated through interpolation of the measured instantaneous altitude h_{corr} as:

$$h_{int}(0) = 120.3 + \frac{120.4 - 120.3}{0.1 - 0.0} * (0 - 0) = 120.3$$

$$h_{int}(520) = 132.5 + \frac{132.6 - 132.5}{523.6 - 519.9} * (520 - 519.9) = 132.5$$

1.3.2. Additional data smoothing

In Table 2, the first and last discrete way points are: $d_a=0m$ and $d_e=799m$, respectively. The altitude data of each discrete way point is smoothed by applying a two steps procedure. The first smoothing run consists of:

$$road_{grade,1}(0) = \frac{h_{int}(200m) - h_{int}(0)}{(0 + 200m)} = \frac{121.0 - 120.3}{200} = 0.0035$$

chosen to demonstrate the smoothing for $d \leq 200m$

$$road_{grade,1}(320) = \frac{h_{int}(520) - h_{int}(120)}{(520) - (120)} = \frac{132.5 - 121}{400} = 0.0288$$

chosen to demonstrate the smoothing for $200m < d < (599m)$

$$road_{grade,1}(720) = \frac{h_{int}(799) - h_{int}(520)}{799 - (520)} = \frac{121.2 - 132.5}{279} = -0.0405$$

chosen to demonstrate the smoothing for $d \geq (599m)$

The smoothed and interpolated altitude is calculated as:

$$h_{int,sm,1}(0) = h_{int}(0) + road_{grade,1}(0) = 120.3 + 0.0035 \approx 120.3m$$

$$h_{int,sm,1}(799) = h_{int,sm,1}(798) + road_{grade,1}(799) = 121.3 - 0.022 = 121.278m$$

Second smoothing run:

$$road_{grade,2}(0) = \frac{h_{int,sm,1}(200) - h_{int,sm,1}(0)}{(200)} = \frac{120 - 120.3}{(200)} = -0.0015$$

chosen to demonstrate the smoothing for $d \leq 200m$

$$road_{grade,2}(320) = \frac{h_{int,sm,1}(520) - h_{int,sm,1}(120)}{(520) - (120)} = \frac{123.7 - 120.2}{400} = 0.0088$$

chosen to demonstrate the smoothing for $200m < d < (599)$

$$road_{grade,2}(720) = \frac{h_{int,sm,1}(799) - h_{int,sm,1}(520)}{799 - (520)} = \frac{121.3 - 123.7}{279} = -0.0086$$

chosen to demonstrate the smoothing for $d \geq (599m)$

1.3.3. Calculation of the final result

The positive cumulative elevation gain of a trip is calculated by integrating all positive interpolated and smoothed road grades, i.e. $road_{grade,2}(d)$. For the presented example the total covered distance was $d_{tot}=139.7$ km and all positive interpolated and smoothed road grades were of 516m. Therefore a positive cumulative elevation gain of $516*100/139.7=370m/100km$ was achieved.

Table 1

Correction of instantaneous vehicle altitude data

Time t [s]	$v(t)$ [km/h]	$h_{GPS}(t)$ [m]	$h_{map}(t)$ [m]	$h(t)$ [m]	$h_{corr}(t)$ [m]	d_i [m]	Cum. d [m]
0	0.00	122.7	129.0	122.7	122.7	0.0	0.0
1	0.00	122.8	129.0	122.8	122.7	0.0	0.0
2	0.00	-	129.1	123.6	122.7	0.0	0.0
3	0.00	-	129.2	124.3	122.7	0.0	0.0
4	0.00	125.1	129.0	125.1	122.7	0.0	0.0
...
18	0.00	120.2	129.4	120.2	120.2	0.0	0.0
19	0.32	120.2	129.4	120.2	120.2	0.1	0.1
...
37	24.31	120.9	132.7	120.9	120.9	6.8	117.9
38	28.18	121.2	133.0	121.2	121.2	7.8	125.7
...
46	13.52	121.4	131.9	121.4	121.4	3.8	193.4
47	38.48	120.7	131.5	120.7	120.7	10.7	204.1
...
56	42.67	119.8	125.2	119.8	119.8	11.9	308.4
57	41.70	119.7	124.8	119.7	119.7	11.6	320.0
...
110	10.95	125.2	132.2	125.2	125.2	3.0	509.0
111	11.75	100.8	132.3	100.8	125.2	3.3	512.2
112	13.52	0.0	132.4	132.4	125.2	3.8	516.0
113	14.01	0.0	132.5	132.5	132.5	3.9	519.9
114	13.36	24.30	132.6	132.6	132.6	3.7	523.6
...
149	39.93	123.6	129.6	123.6	123.6	11.1	719.2
150	39.61	123.4	129.5	123.4	123.4	11.0	730.2
...
157	14.81	121.3	126.1	121.3	121.3	4.1	792.1
158	14.19	121.2	126.2	121.2	121.2	3.9	796.1
159	10.00	128.5	126.1	128.5	121.2	2.8	798.8
160	4.10	130.6	126.0	130.6	121.2	1.2	800.0

- denotes data gaps

Table 2

Calculation of road grade

d [m]	t_0 [s]	d_0 [m]	d_1 [m]	h_0 [m]	h_1 [m]	$h_{map}(d)$ [m]	$road_{grade,i}(d)$ [m/m]	$h_{mr,m,i}(d)$ [m]	$road_{grade,i}(d)$ [m/m]
0	18	0.0	0.1	120.3	120.4	120.3	0.0035	120.3	-0.0015
...
120	37	117.9	125.7	120.9	121.2	121.0	-0.0019	120.2	0.0035
...
200	46	193.4	204.1	121.4	120.7	121.0	-0.0040	120.0	0.0051
...
320	56	308.4	320.0	119.8	119.7	119.7	0.0288	121.4	0.0088
...
520	113	519.9	523.6	132.5	132.6	132.5	0.0097	123.7	0.0037
...
720	149	719.2	730.2	123.6	123.4	123.6	-0.0405	122.9	-0.0086
...
798	158	796.1	798.8	121.2	121.2	121.2	-0.0219	121.3	-0.0151
799	159	798.8	800.0	121.2	121.2	121.2	-0.0220	121.3	-0.0152

Figure 2

The effect of data verification and correction - The altitude profile measured by GPS $h_{GPS}(t)$, the altitude profile provided by the topographic map $h_{map}(t)$, the altitude profile obtained after the screening and principle verification of data quality $h(t)$ and the correction $h_{corr}(t)$ of data listed in Table 1

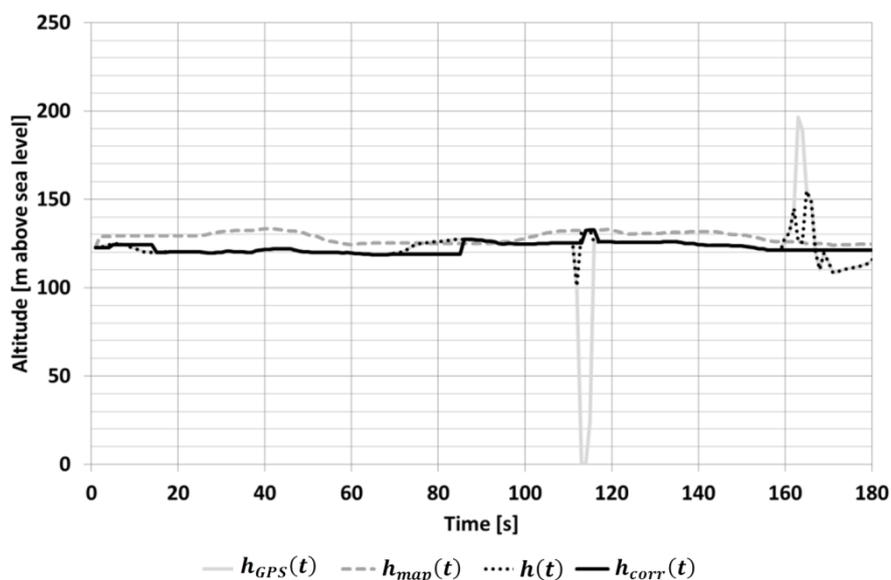


Figure 3

Comparison between the corrected altitude profile $h_{corr}(t)$ and the smoothed and interpolated altitude $h_{int,sm,1}$

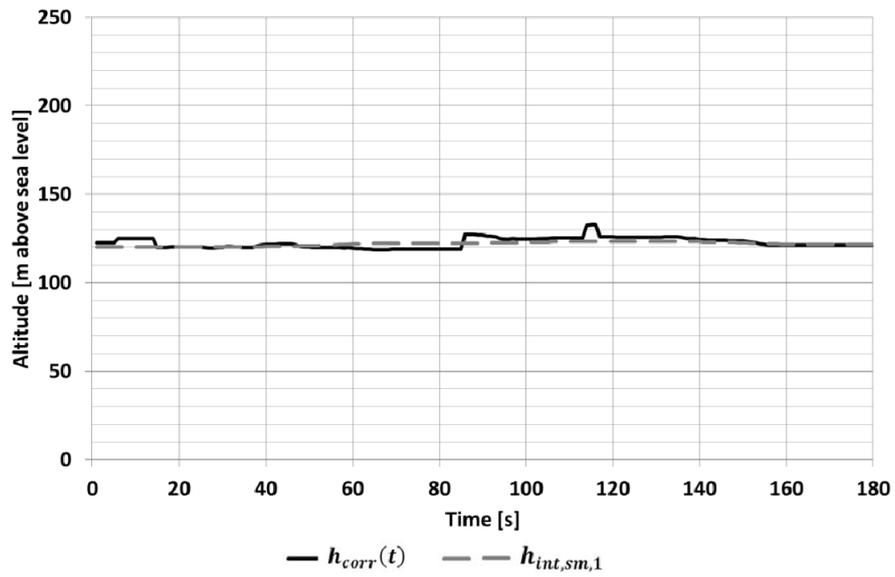


Table 2

Calculation of the positive elevation gain

d [m]	t_0 [s]	d_0 [m]	d_1 [m]	h_0 [m]	h_1 [m]	$h_{int}(d)$ [m]	$road_{grade,1}(d)$ [m/m]	$h_{int,m,1}(d)$ [m]	$road_{grade,2}(d)$ [m/m]
0	18	0.0	0.1	120.3	120.4	120.3	0.0035	120.3	-0.0015
...
120	37	117.9	125.7	120.9	121.2	121.0	-0.0019	120.2	0.0035
...
200	46	193.4	204.1	121.4	120.7	121.0	-0.0040	120.0	0.0051
...
320	56	308.4	320.0	119.8	119.7	119.7	0.0288	121.4	0.0088
...
520	113	519.9	523.6	132.5	132.6	132.5	0.0097	123.7	0.0037
...
720	149	719.2	730.2	123.6	123.4	123.6	-0.0405	122.9	-0.0086
...
798	158	796.1	798.8	121.2	121.2	121.2	-0.0219	121.3	-0.0151
799	159	798.8	800.0	121.2	121.2	121.2	-0.0220	121.3	-0.0152

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